

Abstract: If K is a characteristic zero field with finitely generated absolute Galois group, must every elliptic curve over K have infinite rank? I will discuss several approaches to this open problem, via Diophantine geometry, analytic number theory, and additive combinatorics. Time permitting, I will say something about what is known about the inverse Galois-module problem for Mordell-Weil groups.